## DETECTING CARELESS RESPONDING IN IPSATIVE DATA

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## 'IPSATIVE' RESPONSE FORMATS



- Impossible to endorse all desirable alternatives
- Facilitate differentiation and "slow" thinking (Kahneman, 2011)
- Popular since proper scaling methods have become available, e.g. Thurstonian models family (Brown & Maydeu-Olivares, 2011; 2013; 2018; Brown; 2016a; Brown; 2016b)
  - Normative trait scores can be obtained from ipsative data

## CARELESSNESS IN IPSATIVE ASSESSMENTS

- Like any other questionnaires, ipsative questionnaires can be subject to careless responding when respondents are not sufficiently motivated to give their full attention to the questions.
- However, detecting such responding can be more challenging than when using Likert scales
  - modelling of ipsative responses is inherently multidimensional;
  - method factors need to take to account the comparative nature of ipsative responses

## **OBJECTIVES**

To describe and evaluate two alternative strategies for dealing with careless responses in ipsative data:

- (1) identifying (and ultimately removing from the sample) careless responders using 'person fit' indices designed for ipsative formats;
- (2) controlling for careless responding using method factors embedded in the Thurstonian IRT model (Brown & Maydeu-Olivares, 2012).

## EMPIRICAL STUDY

- Bespoke questionnaire for assessing applicants to public sector jobs in the UK
  - measures 24 non-cognitive skills, covering the Big Five domains
  - consists of 276 multidimensional 'graded response' pairs
- Data can be analysed as ordinal or continuous
- Sample.
  - N=1,388 volunteers who participated in a trial



## 'PERSON FIT' INDICES

- Test takers should express preferences in line with their trait scores; for example, if they are higher on trait A than on trait B, they should prefer items measuring A over items measuring B consistently (adjusted for item parameters)
- Comparing observed responses with responses expected under the measurement model
  - We know observed responses to pair of items  $\{a,b\}$  for person i Observed  $\{a,b\}_i$  (for example, =4)
  - We compute observed response according to the Thurstonian model  $\text{Expected}_{\{\text{a.b}\}_i} \text{=} \text{intercept}_{\{\text{a.b}\}} + \text{loading}_{\{\text{a}\}} \text{*TraitA}_i \text{loading}_{\{\text{b}\}} \text{*TraitB}_i$
- For each test taker, 'fit' between their observed responses and their expected responses are measured by summarising either:
  - Discrepancies
  - Concordance

## PERSON FIT AS A MEASURE OF DISCREPANCIES

- Ferrando (2010) proposed a simple person-fit statistic for linear factor models (also known as "congeneric"), "*lco*"
  - Summary of squared differences of observed and expected responses

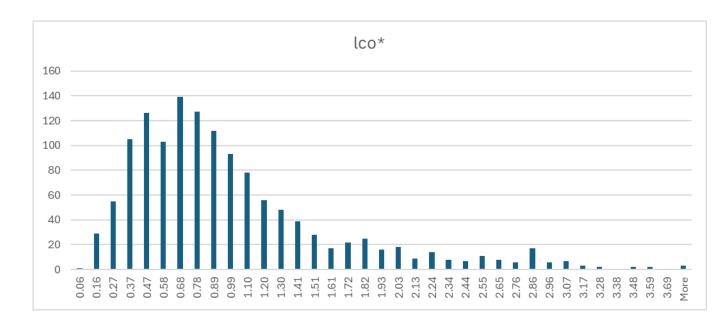
$$lco_i = \sum_{j}^{n} \frac{(X_{ij} - \mu_j - \lambda_j \hat{\theta}_i(ML))}{\sigma^2_{\epsilon j}}^2$$

- *Ico* can be easily extended to Thurstonian factor model
  - The numerator is simply (observed-expected)<sup>2</sup>
  - The denominator (error variance) is constant for all pairs, so can be omitted
  - I suggest computing the mean across 276 pairs rather than the sum

$$lco_i^* = MEAN(Observed_{\{a.b\}_i} - Expected_{\{a.b\}_i})^2$$

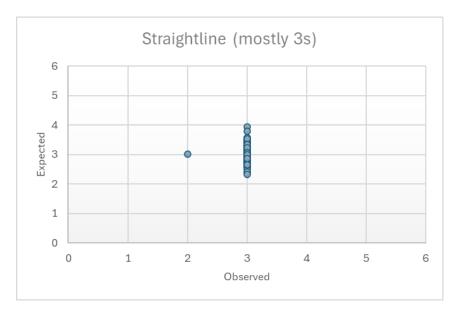
## DISTRIBUTION OF LCO\*

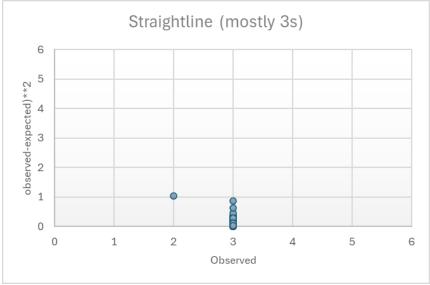
- For the trial sample (before any data cleaning!)
  - We have a long positive tail of outliers (those with large misfit to model)
  - Median = 0.770
  - 5<sup>th</sup> percentile = 0.247
  - 10<sup>th</sup> percentile = 0.311
  - 90<sup>th</sup> percentile = 1.85
  - 95<sup>th</sup> percentile = 2.46



## **PROBLEM**

- With polytomous items, candidates providing midpoint responses will obtain average trait scores
  - Their expected responses will also show central tendency, and will be very similar to their observed responses
- Index lco\* will be very small, suggesting perfect person-fit
- This problem is also described in Ferrando (2010); in single scales, any response pattern using only one or two adjacent categories will have this problem
  - In our case, only patterns with predominant response
     "3" are problematic



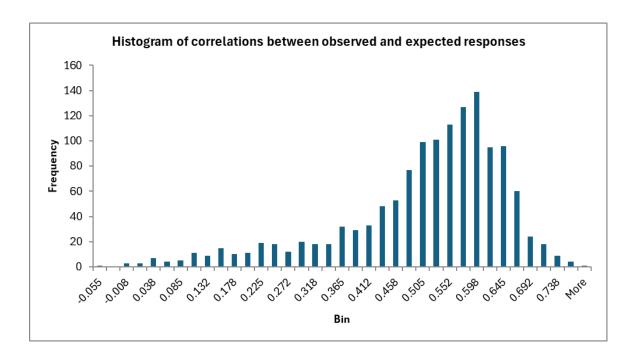


## PERSON FIT AS A MEASURE OF CONCORDANCE

- Pearson's correlation can be computed to capture concordance between observed and expected responses, for each candidate
  - For genuine responses, the correlation should be positive and high
  - For random responses, the correlation should be near zero
  - For central tendency responses, the correlation should be near zero

## DISTRIBUTION OF COR(OBS, EXP)

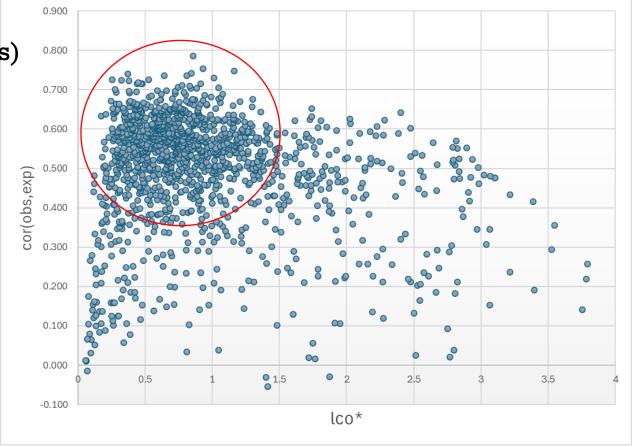
- For our trial sample (before any data cleaning)
  - We have a long negative tail (those with small concordance with the model)
  - Median(cor) = 0.532
  - 5<sup>th</sup> percentile = 0.170
  - 10<sup>th</sup> percentile = 0.280
  - 90th percentile = 0.642
  - 95<sup>th</sup> percentile = 0.664



## DO THE PERSON FIT INDICES AGREE?

Not really (only for careful responders)

- They complement each other for detecting careless responders, who have either:
  - high lco\*
  - or low cor(obs,exp)
  - or both



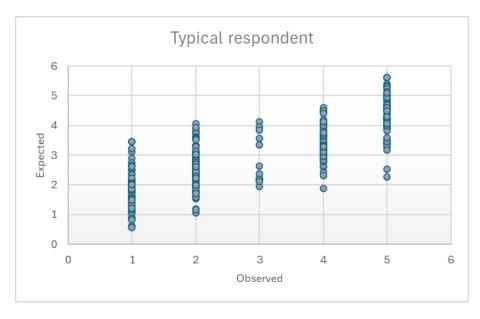
#### EXAMPLE: TYPICAL LCO\* AND COR

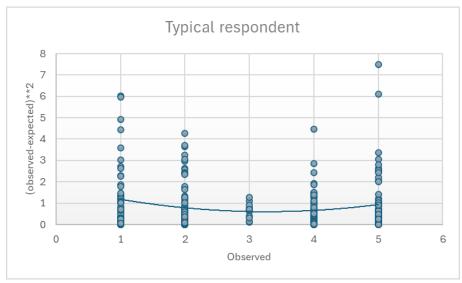
MEAN\_RESPONSE 3.01

SD\_RESPONSE 1.49

*lco*\* 0.858

**cor(obs, exp)** 0.785





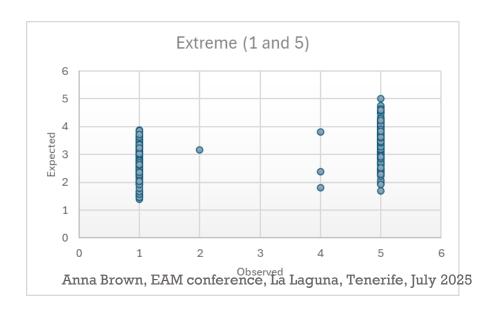
#### EXAMPLE: OUTLIERS ACCORDING TO LCO\*

MEAN\_RESPONSE 3.17

SD\_RESPONSE 1.99

*lco\** 3.105

**cor(obs, exp)** 0.475

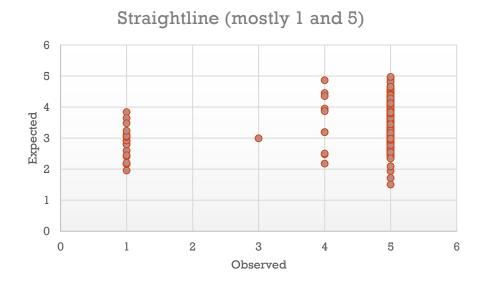




SD\_RESPONSE 1.00

*lco\** 2.687

cor(obs, exp) 0.247



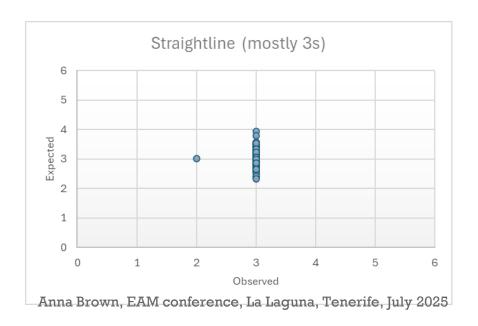
## EXAMPLE: OUTLIERS ACCORDING TO COR(OBS, EXP)

MEAN\_RESPONSE 3.00

SD\_RESPONSE 0.06

*lco\** 0.058

cor(obs, exp) 0.011

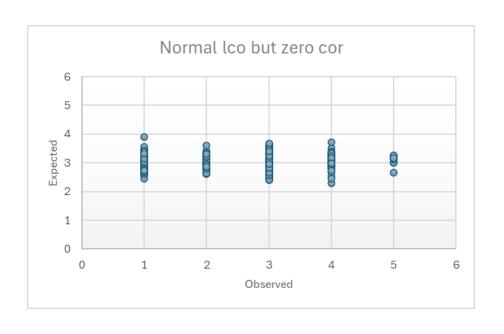


 MEAN\_RESPONSE
 2.85

 SD\_RESPONSE
 0.99

 lco\*
 1.040

 cor(obs, exp)
 0.038



## EXAMPLE: RANDOM RESPONSES

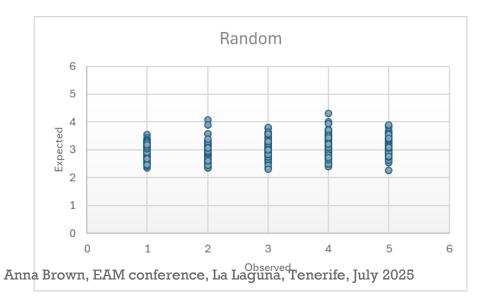
#### Computer generated

MEAN\_RESPONSE 2.98

SD\_RESPONSE 1.419

lco\* 1.897

cor(obs, exp) 0.242



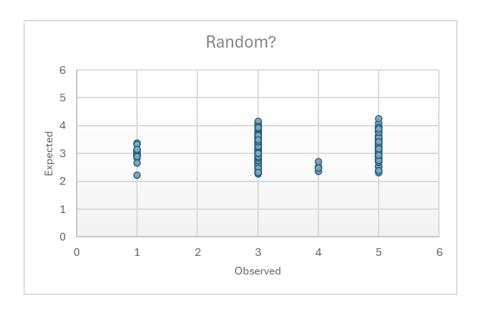
#### Respondent generated

MEAN\_RESPONSE 3.51

SD RESPONSE 1.11

lco\* 1.221

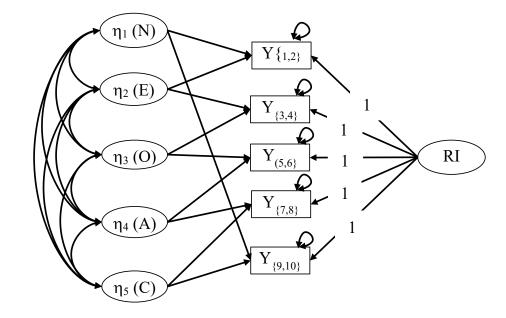
cor(obs, exp) 0.311



## 'METHOD' FACTOR

 A 'random intercept' can be added to the Thurstonian factor model to control carelessness expressed as overusing one response option

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\begin{split} & \operatorname{Expected}_{\{\mathbf{a}.\mathbf{b}\}i} = \\ & = \operatorname{intercept}_{\{\mathbf{a}.\mathbf{b}\}} + \operatorname{rand.intercept}_i + \\ & + \operatorname{loading}_{\{\mathbf{a}\}} * \operatorname{TraitA}_i - \operatorname{loading}_{\{\mathbf{b}\}} * \operatorname{TraitB}_i \end{split}
```



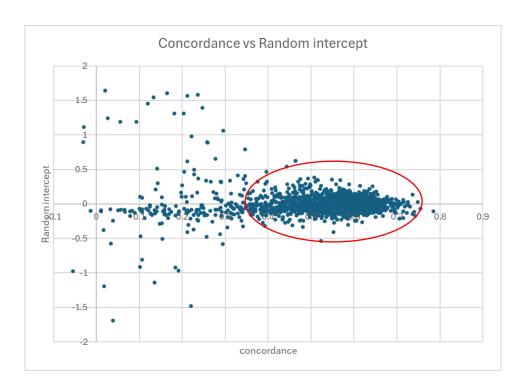
## RANDOM INTERCEPT MODEL RESULTS

- The RI factor had variance 0.054 (p < .001)
  - 5.4% of the substantive traits' variances
  - explained approx. 4% variance of observed responses
- Goodness of fit
  - baseline Thurstonian model (N=1,388): SRMR = .068
  - Thurstonian model with RI (N=1,388): SRMR = .055
  - baseline Thurstonian model without careless responders detected with *lco\** and *cor* (N=1,245): SRMR = .063

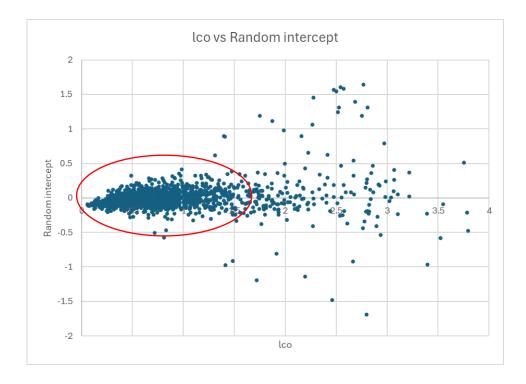
## DO PERSON FIT INDICES AND RI AGREE?

Not really (only for careful responders)

corr(cor, RI) = -.052



corr(lco, RI) = .190



## **CONCLUSIONS**

- No single index is 100% effective at detecting all types of careless responses
- At the individual level, the measures of discrepancy, concordance and random intercept agreed only for careful responders
  - "All happy families are alike; each unhappy family is unhappy in its own way" (L. Tolstoy)
- Combination of lco\* and cor(obs,exp) work for detecting
  - Random responding
  - Straight-lining (any category)
  - Over-using a category or several categories
- Method (RI) factor works for detecting (and controlling for)
  - Over-using one category

## RECOMMENDATIONS

- Determine cut-offs for lco\* and cor indices empirically on your data
- Implement these cut-offs for flagging careless responders
- But consider also implementing simple prevention measures during the test administration, for example:
  - Allow only a certain proportion of responses in certain category, for example, no more than 20% of "equally true" (the middle category)
  - Warn the test taker that they should not select too many responses in the middle category, and when they exceed the limit, warn them that their profile will be void



# THANK YOU! ANY COMMENTS OR QUESTIONS?

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