

# Bootstrap-F and adjusted F-tests in split-plot designs: The effect of non-sphericity and heterogeneity on Type I error

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## Poster

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## Abstract

**Background.** Adjusted F-tests are not robust to simultaneous violation of the assumptions of sphericity and homogeneity of covariance matrices when group sizes are unequal. As an alternative, the bootstrap-F (B-F) method has been proposed. **Objective.** The aim of the study was to analyse the robustness of the Greenhouse-Geisser (F-GG) and Huynh-Feldt (F-HF) tests and the B-F method in split-plot designs under non-sphericity and heterogeneity of covariance matrices between groups. It is hypothesized that the B-F method will outperform the F-GG and F-HF tests. **Method.** A simulation study was conducted using a split-plot design with two groups and three repeated measures under normal distribution. The manipulated variables were: (a) total sample size, (b) group size, (c) epsilon value (Greenhouse-Geisser estimation), (d) coefficient of sample size variation, (e) homogeneity/heterogeneity of covariance matrices and (f) pairing between group size and covariance matrices (null, positive and negative). Type I error rates for time and interaction effects were computed and results were interpreted according to Bradley's liberal criterion, whereby a procedure is robust if the Type I error rate is between 2.5% and 7.5%. **Results.** Adjusted F-tests for time and interaction effects were conservative with positive pairing (variance heterogeneity) and a moderate or high coefficient of sample size variation. They were liberal with negative pairing (variance heterogeneity) and a moderate or high coefficient of sample size variation. The B-F method was robust in all conditions when the coefficient of sample size variation was low or moderate. However, with a high coefficient of sample size variation and negative pairing, the B-F method was robust only when  $N > 20$ . Non-sphericity had little effect on the Type I error rates of all statistics. **Conclusions.** The B-F method showed greater robustness than did the F-GG and F-HF tests, making it a valid option for analysing split-plot designs under heterogeneity of covariance matrices in the conditions studied here. Sample size above 20 is recommended. This research was supported by grant PID2020-113191GB-I00 from the MCIN/AEI/10.13039/501100011033.

## Keywords

Bootstrap, measures repeated, Greenhouse-Geisser, Huynh-Feldt

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